CAR

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**Abstract**

This paper focuses on building a rocket-type car powered by an engine using an elastic air-filled toy balloon as the energy source, determining how distance travelled by the car and efficiency depend on relevant parameters and maximizing them.

Balloon observations were done using a piston inflation/deflation model to calculate energy input, output and rubber stretching losses. Car motion was observed and initial condition parameters (volume and pressure), different jet diameters and nozzle angles were taken into consideration.

**Piston model**

As the balloon deflates pressure, volume and the number of molecules in it change. Therefore, imagine a piston containing all air later used for inflation to which the balloon is attached to. Moving the piston slowly inflates the balloon and releasing it results in spontaneous balloon deflation.

Initial system state is , being the atmospheric pressure, balloon volume before inflation and piston volume.

Ideal gas law equation states that at every moment where is the changing balloon volume and the piston volume, is the gas constant.

Final state is where is the final balloon pressure and the final volume (figure 1).

Integrating initial to final state of gives both inflation and deflation work as the same equations are valid. Energy needed for inflation and gained from deflation is:

where are the known conditions and is determined experimentally for both processes separately.



Figure 1: Piston model at initial and final state for inflation, valid also for deflation with inverted markings (left and right) provides a way to evaluate initial input energy and rubber losses.

**Balloon inflation/deflation**

Pressure was measured using a digital pressure sensor (resolution , possible calibration) at different volumes. Balloon volume was indirectly calculated by taking photos) at known pressures, marking the balloon edge coordinates to find a shape (radius/height) function and numerically integrating this function (using shape rotation). These data give us the overpressure/volume relation shown in figure 2, where the deflation curve is under the inflation curve as expected due to energy losses from rubber deformation and elastic rubber hysteresis is observable.

This experimental results can be explained by balloon elastic energy where is relative strain and is a rubber property.

 [1]

Work needed to increase radius from *r* to *r+dr* under pressure difference (being overpressure) is:

These equations were used to plot a regression, explain and confirm the obtained overpressure/strain curve (figure 2).

Figure 2: Left graph shows the elastic hysteresis of rubber. Gradual inflation and deflation curve differ and the energy is partly dissipated due to material plasticity. Right graph is a fit of elastic energy theoretical model to the experimental results which explains the initial maximum and gradual overpressure drop as the volume continues to increase.

Surface under the volume/pressure curve enlarges with greater initial volume and so do the input and output energy. Efficiency of the balloon is the ratio between deflation energy (work that can be later used to power the car) and inflation energy. Both of them are according to the piston model energies of the initial and final conditions plus surfaces under the curves of these processes.

Maximising travelled distance is having the greatest possible energy after deflation (input energy), and maximizing the efficiency of the balloon is a comparison of remaining energy after deflation and total input energy for inflation (figure 3).

Figure 3: Left graph shows the increase of total energy with volume increase and the right graph showing the decrease of efficiency with volume increase (more rubber losses).

**Construction and motion observation**

Car consists of a plastic cart (length ~ 12 cm), styrofoam base for a plastic tube (d = 2,9 cm) and metal jets / cardboard nozzles, attached at the tube end (figure 4). Car mass is ~ 120 g. This car was placed on metal rails with distance scale to enable us its position determination and keep the movement straight.

A car with filled air-balloon was placed on the rails and a video of its motion was taken with a 120 fps camera. This video was later analysed to find distance/time coordinates and create a graph.

A computer program which analyses these coordinates with a 5 data points frame was created. This program fits a linear or cubic polynomial on the first 5 data points, derives this function and returns the value for the middle point. Frame than moves to the second point taking 2nd to 6th coordinate and repeats the procedure. The result of it is a velocity/time graph on which the initial accelerated motion caused by deflation is easily distinguished from the deceleration part when the car moves due to maximal velocity reached in deflation (figure 4).

Travelled distance is , being the acceleration path distance in which the maximal velocity is reached (determined from the video) and being the deceleration path. The deceleration path was simply calculated with the presented equation in which both and are read from the graph (the latter as the linear coefficient from deceleration).

Figure 4: Final car model photo on the right and a velocity/time graph on the left. After the video analysis, distance/time coordinates were obtained and derived using a program especially created for this purpose.

**Motion description equations**

Input energy defined previously is used for inflatio and it is transformed into kinetic energy of the air molecules during deflation. Losses firstly occur due to resistance to movement (mutual collisions).

Momentum conservation states , and being the air mass and velocity respectively, being the total friction force (air resistance, rolling friction) and and being the car mass and velocity respectively.

Simplified model describes the air behavior taking the mass inside the balloon as

 , being the average pressure evaluated from graphs, balloon volume, *M* air relative atomic mass. Flow at the tube end is here aproximately described according to Bernoulli's principle, neglecting the fluid viscosity in that part so the air velocity is , being air density. Friction force’s main source is air drag due to car shape and its duration is given from flow rate/volume relation as . Momentum conservation equation is simplified to .

**Figure 5: Left graph is the representation of the maximum velocity achievable at a certain volume. Regression expression for Initial volume/maximal velocity relation is obtained using presented equations. Right graph is the total efficiency initial volume relation. It is defined with ratio of final kinetic energy and total input energy (as in the piston model).**

**Jets and nozzles**

Jets are metal circular tube openings which vary the diameter of the tube end. Jet diameter changes how much is the air directed, time needed for deflation, air drag force duration and the amount of resistance air molecules endure in mutual collisions. Flow inside the tube is turbulent with the estimated Reynolds number at the order of magnitude 105. Experiment was conducted for different diameters to find the maximum value as both traveled distance and efficiency depend on .

Nozzles are cardboard cone shaped extensions attached to the tube end to increase the effective velocity, horizontal component of rapid molecules movement. Different nozzles have different angles, changing how much is the air directed but also different tube length as one cone end has a fixed (tube) diameter and thus the amount of losses due to friction changes. Analogous to the jet diameter – maximal velocity relation, the best cone angle also depends on as it was earlier explained.

Best jet diameter and nozzle angle were found to be from 1.2 cm to 1.4 cm and from 15° to 20° respectively for this tube and conditions (figure 6).

**Figure 6: Left graph shows that the travelled distance/jet diameter curve has a maximum which is same for the efficiency as both of these sizes depend on . Analogous to it the right graph has a maximal value too, also valid for travelled distance due to relation.**

**Discussion and conclusion**

These experiments were conducted on a single car design, neglecting the possible influence of a more aerodynamic shape though the friction force as defined in motion description depends on the balloon size creating the air drag. Rolling friction is negligible in comparison to air drag friction and thus other wheels or moving mechanisms are not observed. Nozzle angle optimisation is also presented for a single nozzle shape (cone) and other shapes were not taken into consideration. These possible parameters have been in the initial experiments shown to be of less relevance than the balloon observation.

Balloon was described with a piston inflation/deflation model which was verified by comparing the theory for stretching losses with an experimental curve. The basic working principle was explained and maximum conditions for jets and nozles are found. Longest travelled distance optimised with all parameters (maximal volume before breakage 4.5 dm3, best jet and nozzle) is 70 m and the highest efficiency (minimal volume to start 1.5 dm3, best jet and nozzle) is 6.4%.

References

[1] Y. Levin, F. L. da Silveira, Two rubber balloons: Phase diagram of air transfer, PHYS. REV. E (2004), Volume 69, Issue 5